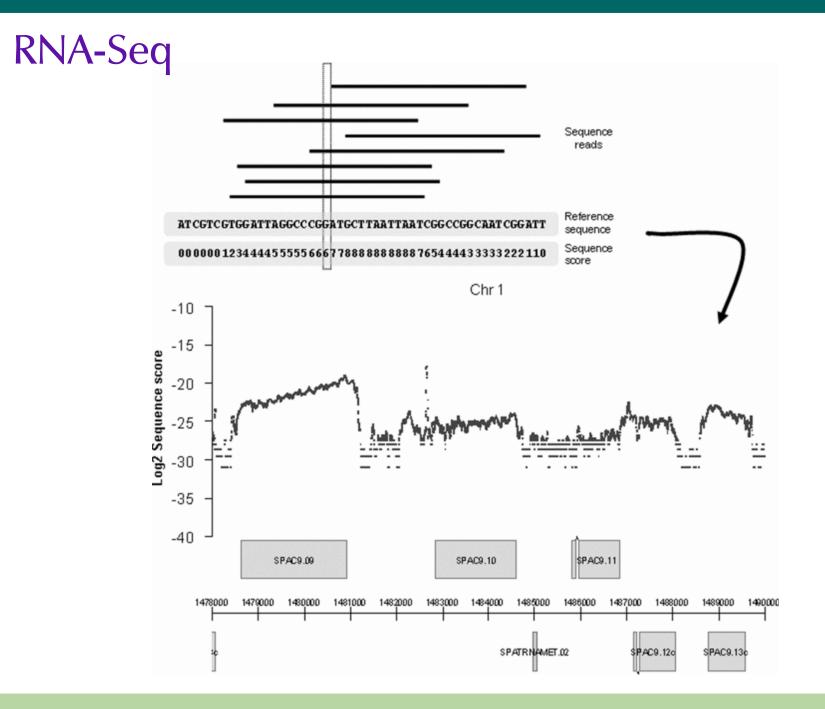
Differential expression analysis for sequencing count data

Simon Anders





Two applications of RNA-Seq

• Discovery

- find new transcripts
- find transcript boundaries
- find splice junctions

Comparison

Given samples from different experimental conditions, find effects of the treatment on

- gene expression strengths
- isoform abundance ratios, splice patterns, transcript boundaries





Should one align against the genome or the transcriptome?

against transcriptome

• easier, because no gapped alignment necessary

but:

risk to miss possible alignments!



Count data in HTS

- RNA-Seq
- Tag-Seq

Gene	GliNS1	G144	G166	G179	CB541	CB660
13CDNA73	4	0	6	1	0	5
A2BP1	19	18	20	7	1	8
A2M	2724	2209	13	49	193	548
A4GALT	0	0	48	0	0	0
AAAS	57	29	224	49	202	92
AACS	1904	1294	5073	5365	3737	3511
AADACL1	3	13	239	683	158	40
[]						

- ChIP-Seq
- Bar-Seq

•••



Counting rules

- Count reads, not base-pairs
- Count each read at most once.
- Discard a read if
 - it cannot be uniquely mapped
 - its alignment overlaps with several genes
 - the alignment quality score is bad
 - (for paired-end reads) the mates do not map to the same gene

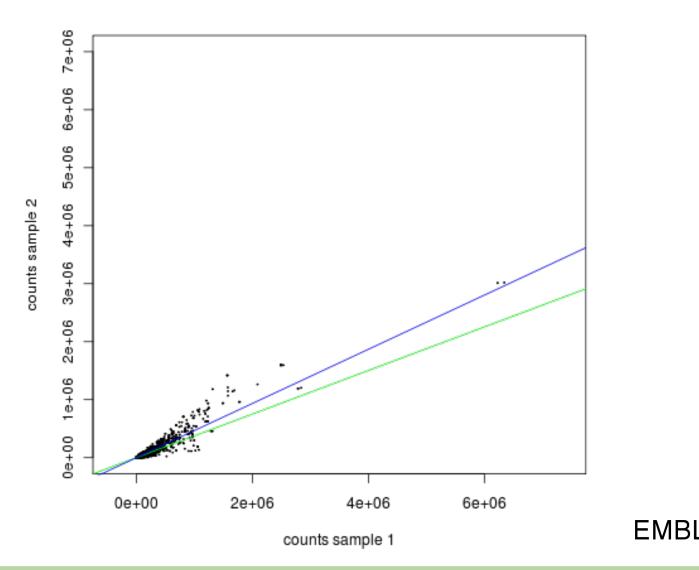


Normalisation for library size

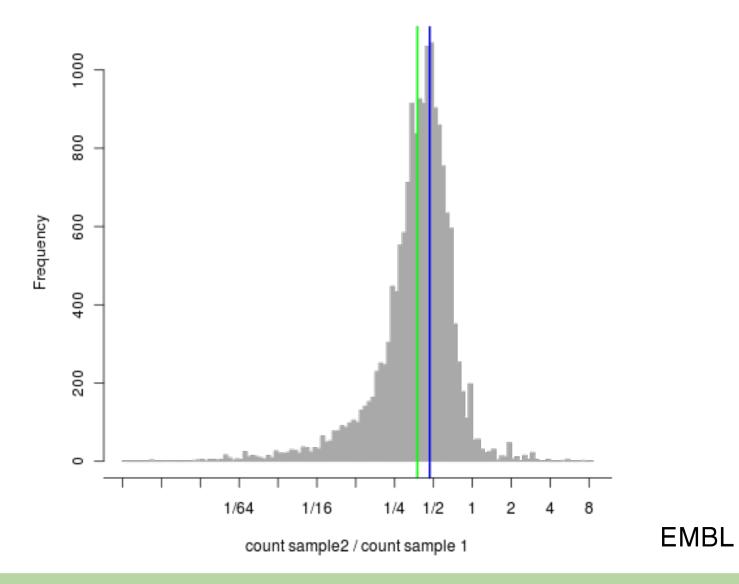
- If sample A has been sampled deeper than sample B, we expect counts to be higher.
- Simply using the total number of reads per sample is not a good idea; genes that are strongly and differentially expressed may distort the ratio of total reads.
- By dividing, for each gene, the count from sample A by the count for sample B, we get one estimate per gene for the size ratio or sample A to sample B.
- We use the median of all these ratios.



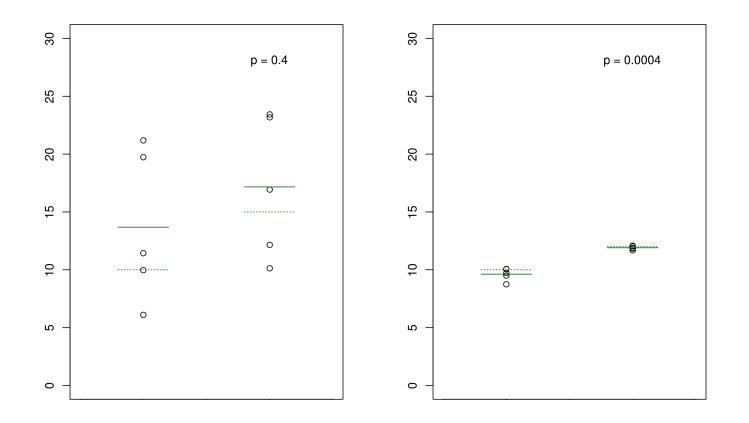
Normalisation for library size



Normalisation for library size



Effect size and significance

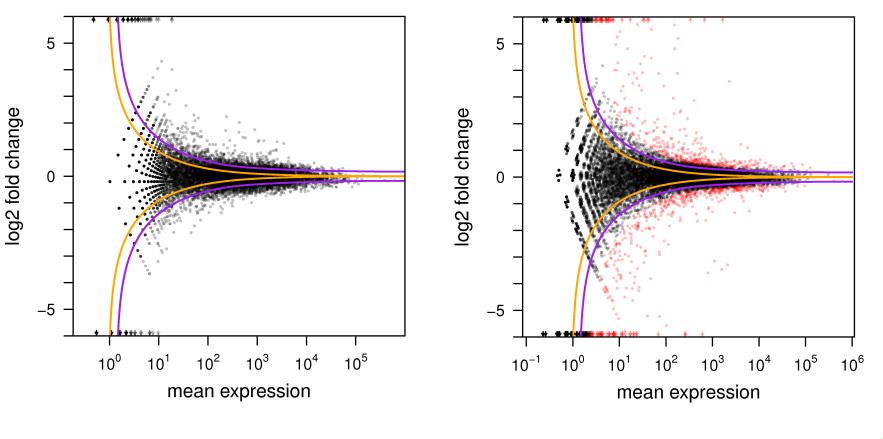




Sample-to-sample variation

comparison of two replicates

comparison of treatment vs control



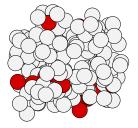


The Poisson distribution



This bad contains very many small balls, 10% of which are red.

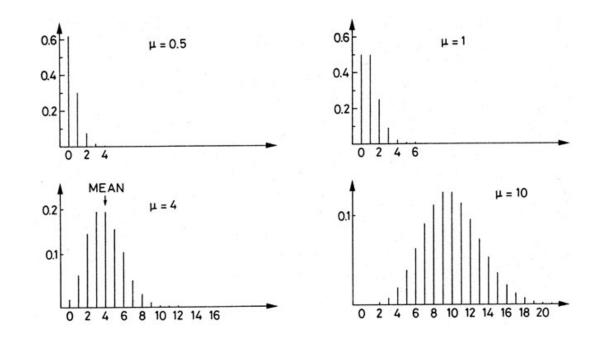
Several experimenters are tasked with determining the percentage of red balls.



Each of them is permitted to draw 20 balls out of the bag, without looking.



- The Poisson distribution turns up whenever things are counted
- Example: A short, light rain shower with *r* drops/m².
 What is the probability to find *k* drops on a paving stone of size 1 m²?



EMB

3/20 = 15%

1/20 = 5%

2/20 = 10%

0/20 = 0%





10 / 100 = 10%

8/100 = 8%

11/100 = 11%

7/100 = 7%

Poisson distribution

- If *p* is the proportion of red balls in the bag, and we draw n balls, we expect μ=pn balls to be red.
- The actual number k of red balls follows a *Poisson* distribution, and hence k varies around its expectation value μ with standard deviation $\sqrt{\mu}$.
- Our estimate of the proportion $\hat{p} = k/n$ hence has the expected value $\mu/n = p$ and the standard error $\Delta p = \sqrt{\mu}/n = p / \sqrt{\mu}$. The relative error is $\Delta p/p = 1 / \sqrt{\mu}$.

balls drawn	expected number of red balls	relative error of estimate
20	2	$1/\sqrt{2} = 71\%$
100	10	$1/\sqrt{10} = 32\%$



Poisson distribution: Counting uncertainty

expected number of red balls	standard deviation of number of red balls	relative error in estimate for fraction of red balls
10	$\sqrt{10} = 3.2$	$1/\sqrt{10} = 31.6\%$
100	$\sqrt{100} = 10.0$	$1/\sqrt{100} = 10.0\%$
1,000	$\sqrt{1,000} = 31.6$	$1/\sqrt{1,000} = 3.2\%$
10,000	$\sqrt{10,000} = 100.0$	$1/\sqrt{10,000} = 1.0\%$



For Poisson-distributed data, the variance is equal to the mean.

Hence, no need to estimate the variance according to several authors: Marioni et al. (2008), Wang et al. (2010), Bloom et al. (2009), Kasowski et al. (2010), Bullard et al. (2010)

Really? Is HTS count data Poisson-distributed?

To sort this out, we have to distinguish *two* sources of noise.



Shot noise

• Consider this situation:

- Several flow cell lanes are filled with aliquots of the *same* prepared library.
- The concentration of a certain transcript species is *exactly* the same in each lane.
- We get the same total number of reads from each lane.
- For each lane, count how often you see a read from the transcript. Will the count all be the same?



Shot noise

• Consider this situation:

- Several flow cell lanes are filled with aliquots of the *same* prepared library.
- The concentration of a certain transcript species is *exactly* the same in each lane.
- We get the same total number of reads from each lane.
- For each lane, count how often you see a read from the transcript. Will the count all be the same?
- Of course not. Even for equal concentration, the counts will vary. This *theoretically unavoidable* noise is called *shot noise*.



Shot noise

- Shot noise: The variance in counts that persists even if everything is exactly equal. (Same as the evenly falling rain on the paving stones.)
- Stochastics tells us that shot noise follows a Poisson distribution.
- The standard deviation of shot noise can be *calculated*: it is equal to the square root of the average count.



Sample noise

Now consider

- Several lanes contain samples from biological replicates.
- The concentration of a given transcript varies around a mean value with a certain standard deviation.
- This standard deviation cannot be calculated, it has to be *estimated* from the data.



Differential expression: Two questions

Assume you use RNA-Seq to determin the concentration of transcripts from some gene in different samples. What is your question?

1. "Is the concentration in one sample different from the expression in another sample?"

Oľ

2. "Can the difference in concentration between treated samples and control samples be attributed to the treatment?"



"Can the difference in concentration between treated samples and control samples be attributed to the treatment?"

Look at the differences between replicates? They show how much variation occurs without difference in treatment.

Could it be that the treatment has no effect and the difference between treatment and control is just a fluctuation of the same kind as between replicates?

To answer this, we need to assess the strength of this sample noise.



Summary: Noise

We distinguish:

- Shot noise
 - unavoidable, appears even with perfect replication
 - dominant noise for weakly expressed genes
- Technical noise
 - from sample preparation and sequencing
 - negligible (if all goes well)
- Biological noise
 - unaccounted-for differenced between samples
 - Dominant noise for strongly expressed genes



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EME

Replicates

Two replicates permit to

• globally estimate variation

Sufficiently many replicates permit to

- estimate variation for each gene
- randomize out unknown covariates
- spot outliers
- improve precision of expression and fold-change estimates



Replicates should differ in *all* aspects in which control and treatment samples differ, except for the actual treatment.

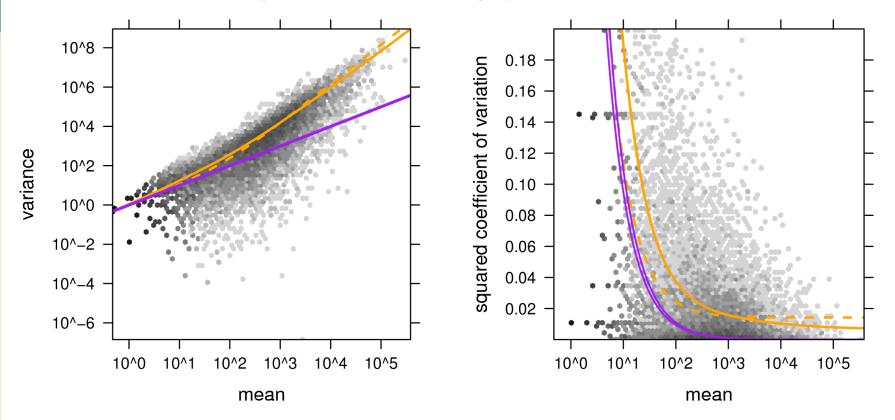


Estimating noise from the data

- If we have many replicates, we can estimate the variance for each gene.
- With only few replicates, we need an additional assumption. We use: "Genes with similar expression strength have similar variance."



Variance depends strongly on the mean



Variance calculated from comparing two replicates

Poisson $v = \mu$ Poisson + constant CV $v = \mu + \alpha \mu^2$ Poisson + local regression $v = \mu + f(\mu^2)$

Technical and biological replicates

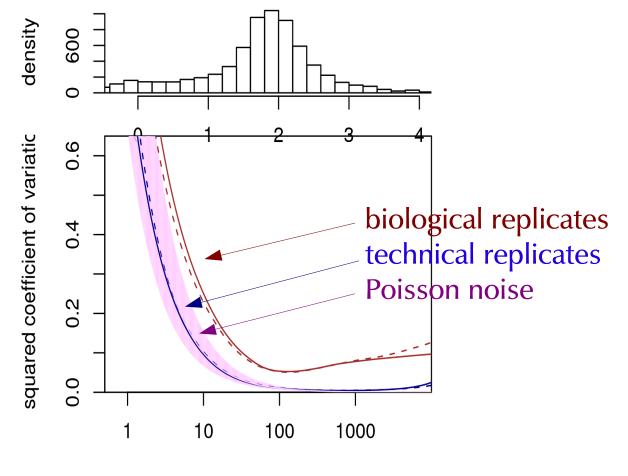
Nagalakshmi et al. (2008) have found that

- counts for the same gene from different *technical* replicates have a variance equal to the mean (Poisson).
- counts for the same gene from different *biological* replicates have a variance exceeding the mean (overdispersion).

Marioni *et al.* (2008) have looked confirmed the first fact (and confused everybody by ignoring the second fact).



Technical and biological replicates



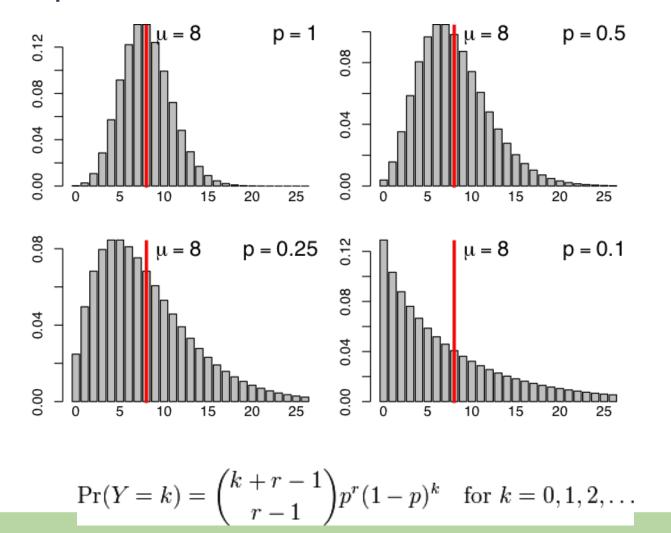
mean

RNA-Seq of yeast [Nagalakshmi et al, 2008]



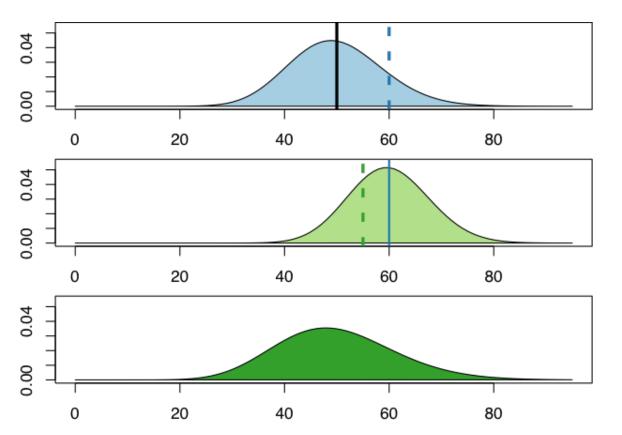
The negative-binomial distribution

A commonly used generalization of the Poisson distribution with *two* parameters





The NB distribution from a hierarchical model



Biological sample with mean μ and variance v

Poisson distribution with mean *q* and variance *q*.

Negative binomial with mean μ and variance q+v.



Testing: Null hypothesis

Model:

The count for a given gene in sample *j* come from negative binomial distributions with the mean $s_j \mu_{\rho}$ and variance $s_j \mu_{\rho} + s_j^2 v(\mu_{\rho})$.

 s_j relative size of library j μ_{ρ} mean value for condition ρ $v(\mu_{\rho})$ fitted variance for mean μ_{ρ}

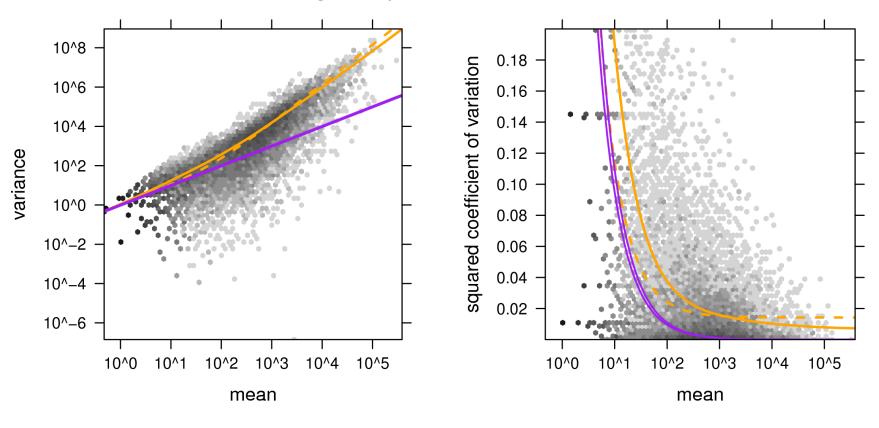
Null hypothesis: The experimental condition r has no influence on the expression of the gene under consideration:

$$\mu_{\rho_1} = \mu_{\rho_2}$$



Model fitting

- Estimate the variance from replicates
- Fit a line to get the variance-mean dependence v(µ) (local regression for a gamma-family generalized linear model, extra math needed to handle differing library sizes)



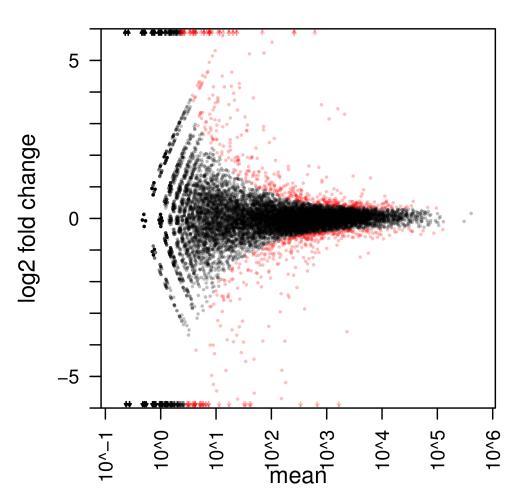
Testing for differential expression

- For each of two conditions, add the count from all replicates, and consider these sums K_{iA} and K_{iB} as NB-distributed with moments as estimated and fitted.
- Then, we calculate the probability of observing the actual sums or more extreme ones, conditioned on the sum being $k_{iA}+k_{iA}$, to get a *p* value.

(similar to the test used in Robinson and Smyth's edgeR)



Differential expression

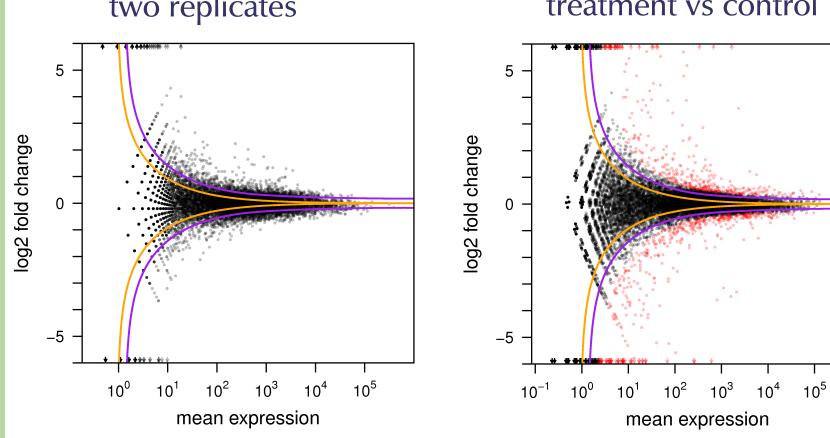


RNA-Seq data: overexpression of two different genes in flies [data: Furlong group]





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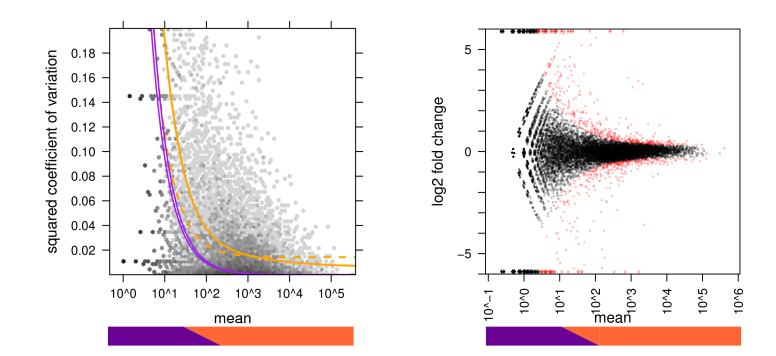


comparison of treatment vs control



comparison of two replicates

Two noise ranges



<u>dominating noise</u> shot noise (Poisson) biological noise How to improve power? deeper sampling more biological replicates EMBL

Further use cases

Similar count data appears in

- comparative ChiP-Seq
- barcode sequencing

• • •

and can be analysed with *DESeq* as well.



Conclusions I

- Proper estimation of variance between *biological* replicates is vital. Using Poisson variance is incorrect.
- Estimating variance-mean dependence with local regression works well for this purpose.
- The negative-binomial model allows for a powerful test for differential expression
- S. Anders, W. Huber: "Differential expression analysis for sequence count data", Genome Biol **11** (2010) R106
- Software (*DESeq*) available from Bioconductor and EMBL web site.



Alternative splicing

- So far, we counted reads in genes.
- To study alternative splicing, reads have to be assigned to *transcripts*.
- This introduces ambiguity, which adds uncertainty.
- Current tools (e.g., *cufflinks*) allow to quantify this uncertainty.
- However: To assess the significance of differences to isoform ratios between conditions, the assignment uncertainty has to be combined with the noise estimates.
- This is not yet possible with existing tools.



Regulation of isoform abundance ratios

- In higher eukaryotes, most genes have several isoforms.
- RNA-Seq is better suited than microarrays to see which isoforms are present in a sample.
- This opens the possibility to study regulation of isoform abundance ratios, e.g.: Is a given exon spliced out more often in one tissue type than in another one?
- We will soon release DEXSeq, a tool to test for differential isoform expression in RNA-Seq data.



Data set used for to demonstrate DEXSeq:

Genome Research

Research

21:193-202 © 2011

Conservation of an RNA regulatory map between *Drosophila* and mammals

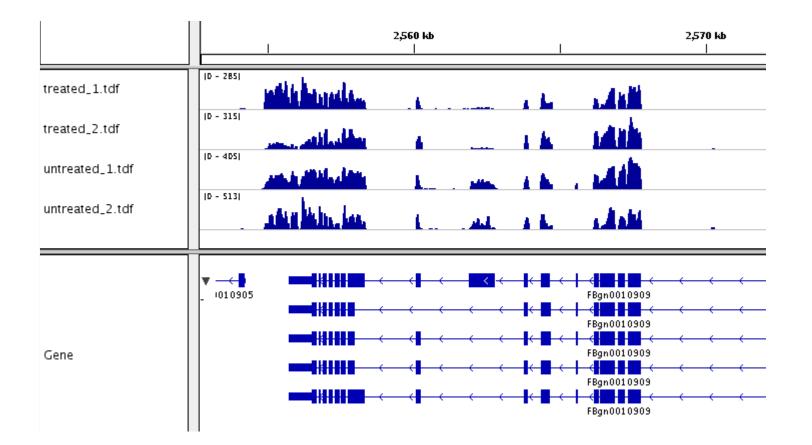
Angela N. Brooks,^{1,7} Li Yang,^{2,7} Michael O. Duff,^{2,3} Kasper D. Hansen,⁴ Jung W. Park,^{2,3} Sandrine Dudoit,^{4,5} Steven E. Brenner,^{1,6,8} and Brenton R. Graveley^{2,3,8}

Drosophila melanogaster S2 cell cultures:

- control (no treatment):
 4 biological replicates (2x single end, 2x paired end)
- treatment: knock-down of pasilla (a splicing factor)
 3 biological replicates (1x single end, 2x paired end)

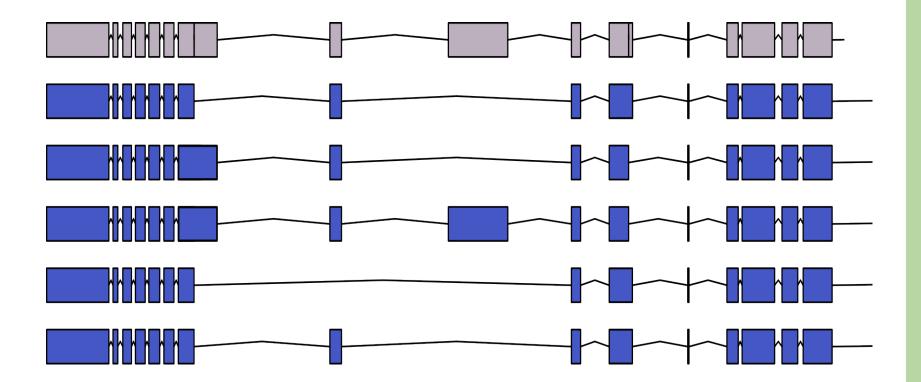


Alternative isoform regulation



Data: Brooks et al., Genome Res., 2010 EMBL

Exon counting bins





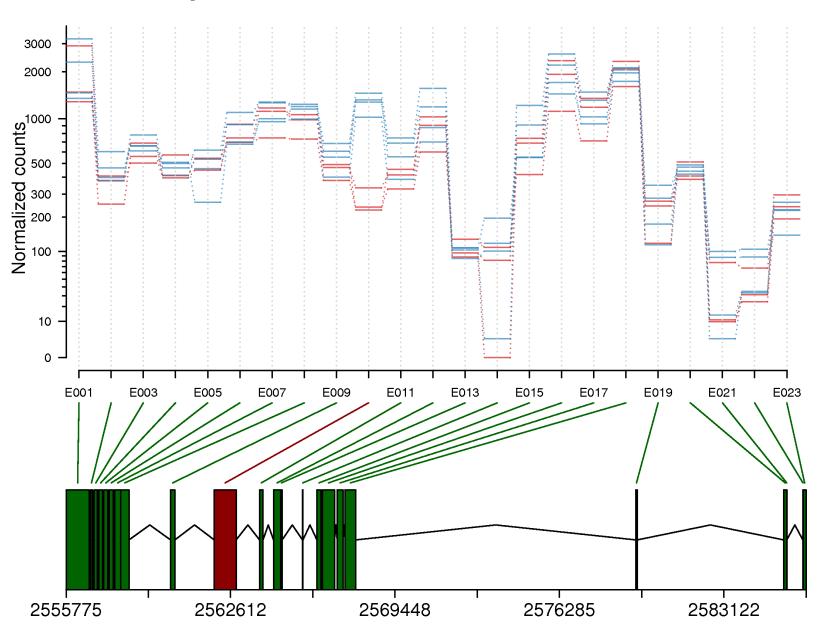
Count table for a gene

[...]

number of reads mapped to each exon (or part of exon) in gene msn:

	$treated_1$	treated_2	$control_1$	control_2	
E01	398	556	561	456	
E02	112	180	153	137	
E03	238	306	298	226	
E04	162	171	183	146	
E05	192	272	234	199	
E06	314	464	419	331	
E07	373	525	481	404	
E08	323	427	475	373	
E09	194	213	273	176	
E10	90	90	530	398	< !
E11	172	207	283	227	
E12	290	397	606	368	< ?
E13	33	48	33	33	
E14	0	33	2	37	
E15	248	314	468	287	
E16	554	841	1024	680	





FBgn0010909 -

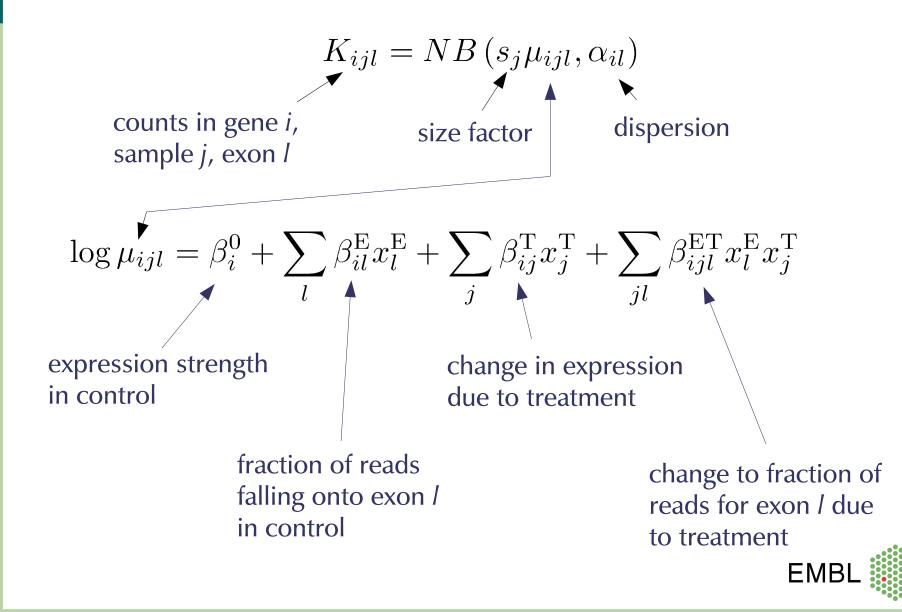
treated untreated

Model

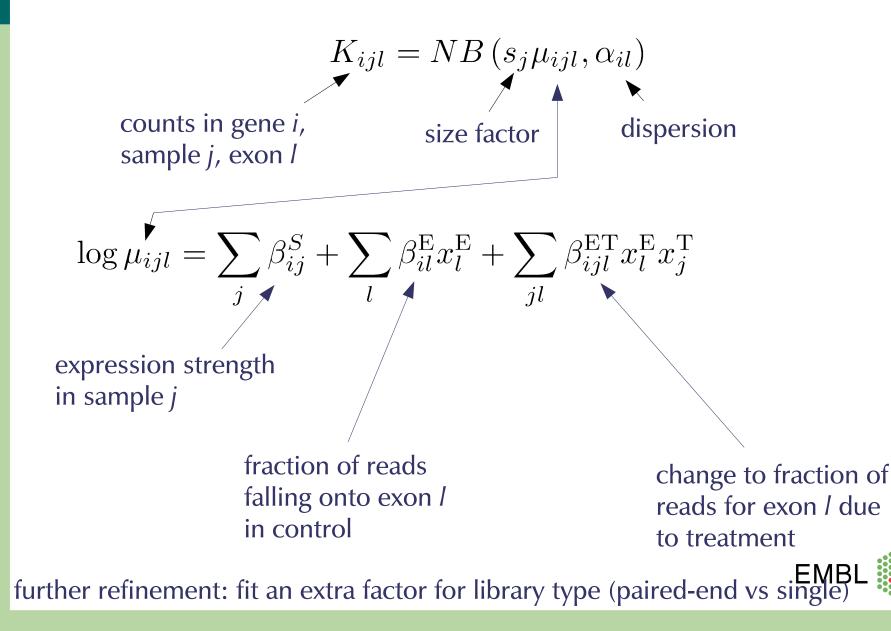
The expected count rate for exon *l* of gene *l* in sample *j* can be modelled as product of

- the baseline (control) expression strength of gene *i*
- the fraction of the reads from gene *i* that overlap with exon *l* under control condition
- the effect of the treatment of sample *j* on the expression strength of gene *I*
- the effect of the treatment of sample *j* on the fraction of the reads from gene *i* that overlap with exon *l*
- the sequencing depth (normalization factor) of sample *j* EMB

Model



Model, refined



Dispersion estimation

- Standard maximum-likelihood estimates for dispersion parameters have very strong bias in case of small sample size.
- A method-of-moments estimator (as used in *DESeq*) cannot be used due to crossed factors.
- We take over the solution from the new *edgeR* version: Cox-Reid conditional-maximum-likelihood estimation

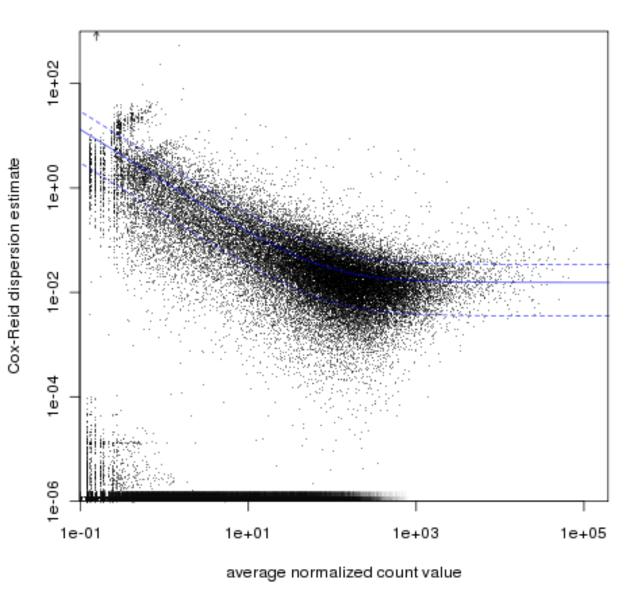
Dispersion estimation

Small sample size, so some data sharing is necessary to get power.

- one value fits all?
- one value for each gene?
- one value for each exon?



Dispersion vs mean

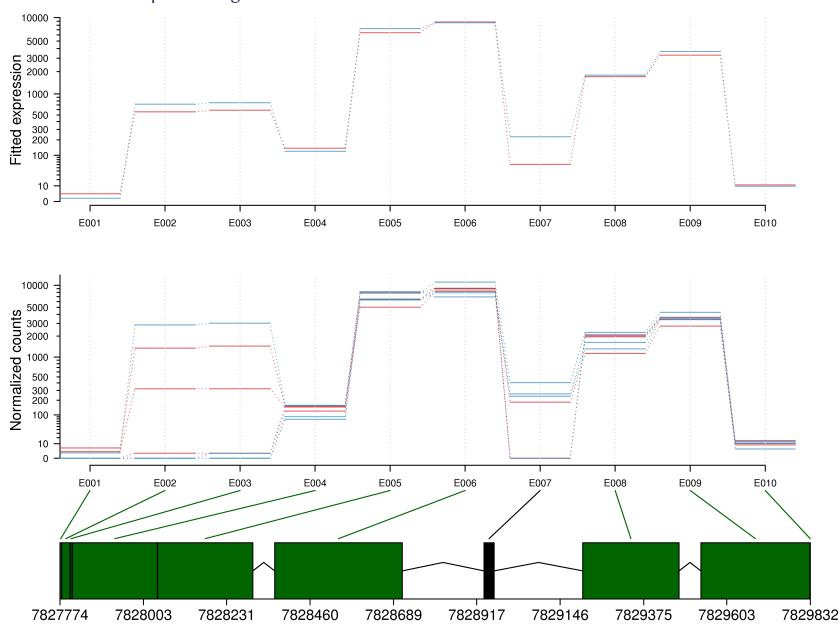




RpS14a (FBgn0004403)

treated

untreated



DEXSeq

- combination of Python scripts and an R package
- Python script to get counting bins from a GTF file
- Python script to get count table from SAM files
- R functions to set up model frames and perform GLM fits and ANODEV
- R functions to visualize results and compile an HTML report
- nearly ready for release



Conclusion II

- Counting within exons and NB-GLMs allows to study isoform regulation.
- Proper statistical testing allows to see whether changes in isoform abundances are just random variation or may be attributed to changes in tissue type or experimental condition.
- Testing on the level of individual exons gives power and might be helpful to study the mechanisms of alternative isoform regulation.
- DEXSeq is nearly ready for release.



Acknowledgements

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- Alejandro Reyes
- Wolfgang Huber

Funding:

• EMBL





HTSeq

A Python package to process and analyse HTS data



HTSeq: Features

- A framework to process and analyse highthroughput sequencing data with Python
- Simple but powerful interface
- Functionality to read, statistically analyse, transform sequences, reads, alignment
- Convenient handling of position-specific data such as coverage vectors, or gene and exon positions
- Well documented, with examples for common use cases.
- In-house support

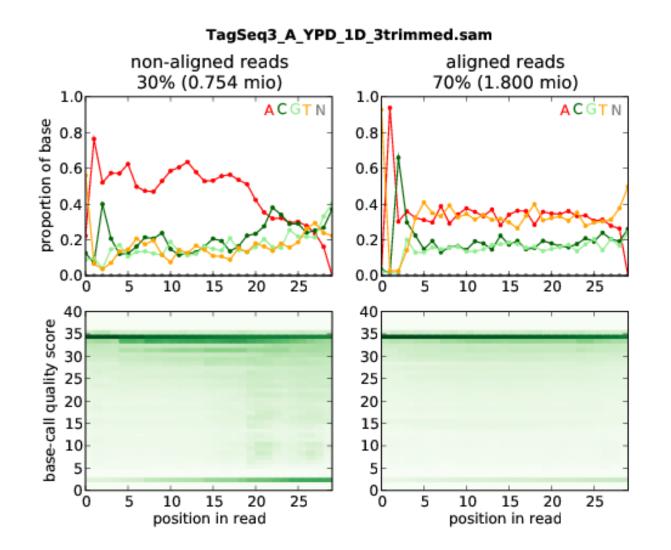


HTSeq: Typical use cases

- Analyse base composition and quality scores for quality assessment of a read
- Trim of adapters in snRNA-Seq
- Calculate coverage vectors for ChIP-Seq
- Assign reads to genes to get count data from RNA-Seq (incl. handling of spliced reads, overlapping genes, ambiguous maps, etc.)
- Split reads according to multiplex tags
- etc.



Quality assessment with HTSeq





HTSeq: Availability

 HTSeq is available from http://www-huber.embl.de/users/anders/HTSeq

• Testers wanted

