# Package ‘globalSeq’

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globalSeq-package  Negative binomial global test

Description

Testing for association between RNA-Seq and other genomic data is challenging due to high variability of the former and high dimensionality of the latter.

Using the negative binomial distribution and a random effects model, we developed an omnibus test that overcomes both difficulties. It may be conceptualised as a test of overall significance in regression analysis, where the response variable is overdispersed and the number of explanatory variables exceeds the sample size.

The proposed method can detect genetic and epigenetic alterations that affect gene expression. It can examine complex regulatory mechanisms of gene expression.

Getting started

omnibus tests entire covariate sets
proprius shows individual contributions
cursus analyses the whole genome

The following command opens the vignette:
utils::vignette("globalSeq")
More information

A Rauschenberger, MA Jonker, MA van de Wiel, and RX Menezes (2016). "Testing for association between RNA-Seq and high-dimensional data", *BMC Bioinformatics*. 17:118. [html pdf](#) (open access)

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## Description

This function tests for associations between gene expression or exon abundance (Y) and genetic or epigenetic alterations (X). Using the locations of genes (Yloc), and the locations of genetic or epigenetic alterations (Xloc), the expression of each gene is tested for associations with alterations on the same chromosome that are closer to the gene than a given distance (window).

## Usage

```r
cursus(Y, Yloc, X, Xloc, window,
       Ychr = NULL, Xchr = NULL,
       offset = NULL, group = NULL,
       perm = 1000, nodes = 2,
       phi = NULL, kind = 0.01)
```

## Arguments

- **Y** - **RNA-Seq data**: numeric matrix with q rows (genes) and n columns (samples); or a SummarizedExperiment object
- **Yloc** - **location RNA-Seq**: numeric vector of length q (point location); numeric matrix with q rows and two columns (start and end locations)
- **X** - **genomic profile**: numeric matrix with p rows (covariates) and n columns (samples)
- **Xloc** - **location covariates**: numeric vector of length p
- **window** - **maximum distance**: non-negative real number
- **Ychr** - chromosome RNA-Seq: factor of length q
- **Xchr** - chromosome covariates: factor of length p
- **offset** - numeric vector of length n
- **group** - confounding variable: factor of length n
- **perm** - number of iterations: positive integer
- **nodes** - number of cluster nodes for parallel computation
- **phi** - dispersion parameters: vector of length q
- **kind** - computation: number between 0 and 1
Details

Note that Yloc, Xloc and window must be given in the same unit, usually in base pairs. If Yloc indicates interval locations, and window is zero, then only covariates between the start and end location of the gene are of interest. Typically window is larger than one million base pairs.

If Y and X include data from a single chromosome, Ychr and Xchr are redundant. If Y or X include data from multiple chromosomes, Ychr and Xchr should be specified in order to prevent confusion between chromosomes.

For the simultaneous analysis of multiple genomic profiles X should be a list of numeric matrices with n columns (samples), Xloc a list of numeric vectors, and window a list of non-negative real numbers. If provided, Xchr should be alist of of numeric vectors.

The offset is meant to account for different library sizes. By default the offset is calculated based on Y. Different library sizes can be ignored by setting the offset to rep(1,n).

The user can provide the confounding variable group. Note that each level of group must appear at least twice in order to allow stratified permutations.

Efficient alternatives to classical permutation (kind=1) are the method of control variates (kind=0) and permutation in chunks (0 < kind < 1) details.

Value

The function returns a dataframe, with the p-values in the first row and the test statistics in the second row.

References

A Rauschenberger, MA Jonker, MA van de Wiel, and RX Menezes (2016). "Testing for association between RNA-Seq and high-dimensional data", BMC Bioinformatics. 17:118. html pdf (open access)


See Also

The function omnibus tests for associations between an overdispersed response variable and a high-dimensional covariate set. The function proprius calculates the contributions of individual samples or covariates to the test statistic. All other function of the R package globalSeq are internal.

Examples

# simulate high-dimensional data
n <- 30; q <- 10; p <- 100
Y <- matrix(rnbinom(q*n,mu=10,size=1/0.25),nrow=q,ncol=n)
X <- matrix(rnorm(p*n),nrow=p,ncol=n)
Yloc <- seq(0,1,length.out=q)
Xloc <- seq(0,1,length.out=p)
window <- 1
# hypothesis testing
cursus(Y, Yloc, X, Xloc, window)

---

**Synopsis**

**Description**

Communicates between *cursus* and *omnibus* by coordinating a chromosome-wide analysis.

**Usage**

```r
intern.chromo(Y, Ystart, Yend, X, Xloc,
   window, offset, group, perm,
   nodes, phi, kind)
```

**Arguments**

- **Y**: RNA-Seq data: numeric matrix with q rows (genes) and n columns (samples); or a SummarizedExperiment object
- **Ystart**: start location of genes: numeric vector of length q
- **Yend**: end location of genes: NULL or numeric vector of length q
- **X**: genomic profile: numeric matrix with p rows (covariates) and n columns (samples)
- **Xloc**: location covariates: numeric vector of length p
- **window**: maximum distance: non-negative real number
- **offset**: numeric vector of length n
- **group**: confounding variable: factor of length n
- **perm**: number of iterations: positive integer
- **nodes**: number of cluster nodes for parallel computation
- **phi**: dispersion parameters: vector of length q
- **kind**: computation: number between 0 and 1

**Value**

The function returns a dataframe, with the p-value in the first column, and the test statistic in the second column.
# Examples

```r
# simulate high-dimensional data
n <- 30
q <- 10
p <- 100
set.seed(1)
Y <- matrix(rnbinom(q*n,mu=10, size=1/0.25),nrow=q,ncol=n)
X <- matrix(rnorm(p*n),nrow=p,ncol=n)
Yloc <- seq(0,1,length.out=q)
Xloc <- seq(0,1,length.out=p)
window <- 1

# hypothesis testing
cursus(Y,Yloc,X,Xloc,window)
```

---

**intern.crude**  
*Internal function*

**Description**

Using the parameter estimates `mu` and `phi` and the permutation matrix `perm`, these functions test for global association between `y` and `X`. The function `intern.crude` calculates p-values by permutation (without repetitions). The functions `intern.focus` and `intern.conva` use different tricks to increase precision and decrease computational expense.

**Usage**

```r
intern.crude(y, X, mu, phi, perm)
intern.focus(y, X, mu, phi, perm, focus)
intern.conva(y, X, mu, phi, perm, offset)
```

**Arguments**

- `y`  
  response variable: numeric vector of length `n`
- `X`  
  covariate set: numeric matrix with `n` rows (samples) and `p` columns (covariates)
- `mu`  
  mean parameters: numeric vector of length `n`
- `phi`  
  dispersion parameter: non-negative real number
- `perm`  
  permutations: matrix with `n` rows (see example)
- `focus`  
  number between 0 and 1
- `offset`  
  numeric vector of length `n`
The function **intern.focus** uses permutations in chunks. If the remaining permutations do not allow to reach a specified significance level, it stops and rounds the p-value to one.

The function **intern.conva** uses the method of control variates from Senchaudhuri et al. (1995). Roughly speaking, if the test statistics from Rauschenberger et al. (2016) and Goeman et al. (2004) are highly correlated, it returns the asymptotic p-value from Goeman et al. (2004).

Each function returns a dataframe, with the p-value in the first row, and the test statistic in the second row.


A Rauschenberger, MA Jonker, MA van de Wiel, and RX Menezes (2016). "Testing for association between RNA-Seq and high-dimensional data", *BMC Bioinformatics*. 17:118. html pdf (open access)


These are internal functions. The user functions of the R package **globalSeq** are **cursus**, **omnibus**, and **proprius**.

# simulate high-dimensional data
n <- 30
p <- 100
# set.seed(1)
y <- rnbinom(n,mu=10,size=1/0.25)
X <- matrix(rnorm(n*p),nrow=n,ncol=p)

# prepare arguments
mu <- rep(mean(y),n)
phi <- (var(y)-mu)/mu^2
perm <- intern.permu(n=n,it=99,group=NULL,kind=1)

# perform tests
intern.crude(y,X,mu,phi,perm)
intern.focus(y,X,mu,phi,perm,focus=0.01)
intern.conva(y,X,mu,phi,perm,NULL)
Description

This function estimates the parameters of the negative binomial distribution by maximum likelihood. It is called by the functions omnibus and proprius.

Usage

```r
intern.estim(y, offset = NULL)
```

Arguments

- `y`: random variable: numeric vector of length n
- `offset`: numeric vector of length n

Details

We assume the negative binomial distribution $y_i \sim \text{NB}(\mu, \phi)$, where the samples are indexed by $i (i=1,\ldots,n)$. Our parametrisation leads to $E[y] = \mu$ and $\text{Var}[y] = \mu + \phi \mu^2$. With an offset the model becomes $y_i \sim \text{NB}(a_i \mu, \phi)$, where the $a_i$ are known.

Value

The function returns a list of numeric vectors.

References

A Rauschenberger, MA Jonker, MA van de Wiel, and RX Menezes (2016). "Testing for association between RNA-Seq and high-dimensional data", BMC Bioinformatics. 17:118. html pdf (open access)

See Also

This is an internal function. The user functions are cursus, omnibus, and proprius.

Examples

```r
set.seed(1)
y <- rnbinom(n=1000, mu=10, size=1/0.2)
intern.estim(y)
```
**intern.matrix**

*Internal function*

**Description**

Convert RNA-Seq data to a numeric matrix

**Usage**

`intern.matrix(Y)`

**Arguments**

- *Y*: RNA-Seq data: numeric matrix with q rows (genes) and n columns (samples); or a SummarizedExperiment object

**Value**

The function returns a matrix.

**Examples**

```r
# simulate RNA-Seq data
Y <- matrix(rnbinom(30, mu=10, size=1/0.2), nrow=10, ncol=3)
rownames(Y) <- paste("gene", 1:nrow(Y), sep="")
colnames(Y) <- paste("cell", 1:ncol(Y), sep="")

# create data structure
# Z <- SummarizedExperiment::SummarizedExperiment(  
#     S4Vectors::SimpleList(counts=Y))

# conversion to matrix
# all.equal(Y, intern.matrix(Z))
```

**intern.permu**

*Internal function*

**Description**

The number of permutations of n elements is n!. This function randomly rearranges the elements it times, and then deletes all duplicates. Thus it finds always less than it and n! permutations. If a confounding variable is provided, the function uses stratified permutation. This function is called by the functions `omnibus` and `proprius`. 
Usage

intern.permu(n, it, group, kind)

Arguments

n  Number of samples.
it  Number of repetitions.
group  Either NULL or a factor of length n.
kind  computation : number between 0 and 1

Value

The function returns a matrix.

References

A Rauschenberger, MA Jonker, MA van de Wiel, and RX Menezes (2016). "Testing for association between RNA-Seq and high-dimensional data", *BMC Bioinformatics*. 17:118. [html pdf](open access)

See Also

This is an internal function. The user functions are *cursus*, *omnibus*, and *proprius*.

Examples

group <- as.factor(c('A','A','B','B','B'))
set.seed(1)
intern.permu(n=5,it=1000,group=group,kind=1)

---

intern.plot  

Internal function

Description

This function plots the individual contributions to the test statistic. It is called by the function *proprius*.

Usage

intern.plot(u, upper = NULL, xlab = "indices")

Arguments

u  influence: numeric vector of length n
upper  critical values: numeric vector of length n
xlab  label of horizontal axis: character string
**Value**

The function plots the arguments.

**References**

A Rauschenberger, MA Jonker, MA van de Wiel, and RX Menezes (2016). "Testing for association between RNA-Seq and high-dimensional data", *BMC Bioinformatics*. 17:118. [html pdf](#) (open access)

**See Also**

This is an internal function. The user functions are `cursus`, `omnibus`, and `proprius`.

**Examples**

```r
# simulate influences
set.seed(1)
u <- rchisq(n=100, df=2)

# influence plot
upper <- rep(qchisq(p=0.95, df=2), times=100)
intern.plot(u, upper)
```

---

**intern.sam**

Internal function

**Description**

These functions calculate the contribution of covariate or samples to the test statistic. They are called by the function `proprius`.

**Usage**

```r
intern.sam(y, X, mu, phi)
intern.cov(y, X, mu, phi)
```

**Arguments**

- `y`: response variable; numeric vector of length `n`
- `X`: covariate set; numeric matrix with `n` rows (samples) and `p` columns (covariates)
- `mu`: mean parameters; numeric vector of length `n`
- `phi`: dispersion parameter; non-negative real number

**Value**

Both functions return a numeric vector.
References

A Rauschenberger, MA Jonker, MA van de Wiel, and RX Menezes (2016). "Testing for association between RNA-Seq and high-dimensional data", BMC Bioinformatics. 17:118. html pdf (open access)


See Also

This is an internal function. The user functions of the R package globalSeq are cursus, omnibus, and proprius.

Examples

# simulate high-dimensional data
n <- 30
p <- 100
set.seed(1)
y <- rnbinom(n,mu=10,size=1/0.25)
X <- matrix(rnorm(n*p),nrow=n,ncol=p)

# prepare arguments
mu <- rep(mean(y),n)
phi <- (var(y)-mean(y))/mean(y)^2

# decompose test statistic
intern.sam(y,X,mu,phi)
intern.cov(y,X,mu,phi)

Description

This function calculates the test statistic. It is called by the function omnibus.

Usage

intern.score(y, R, mu, phi)

Arguments

y      response variable: numeric vector of length n
R      numeric matrix of dimensions n*n (see example)
mu     mean parameters: numeric vector of length 1 or n
phi    dispersion parameter: non-negative real number
**Value**

The function returns a real number.

**References**

A Rauschenberger, MA Jonker, MA van de Wiel, and RX Menezes (2016). "Testing for association between RNA-Seq and high-dimensional data", *BMC Bioinformatics*. 17:118. [html](#) [pdf](#) (open access)

**See Also**

This is an *internal* function. The user functions are *cursus*, *omnibus*, and *proprius*.

**Examples**

```r
# simulate high-dimensional data
n <- 30
p <- 100
set.seed(1)
y <- rnbinom(n,mu=10,size=1/0.25)
X <- matrix(rnorm(n*p),nrow=n,ncol=p)

# calculate test statistic
R <- X %*% t(X) / ncol(X)
mu <- mean(y)
phi <- (var(y)-mu)/mu^2
intern.score(y,R,mu,phi)
```

---

**Description**

Communicates between *cursus* and *omnibus* by selecting the covariates of interest.

**Usage**

```r
intern.select(i, Y, Ystart, Yend, X, Xloc, window, offset, group, perm, phi, kind)
```

**Arguments**

- `i`  
  index
- `Y`  
  RNA-Seq data: numeric matrix with q rows (genes) and n columns (samples); or a SummarizedExperiment object
- `Ystart`  
  location (or start location)
Yend | location (or end location)
--- | ---
X | genomic profile: numeric matrix with \( p \) rows (covariates) and \( n \) columns (samples)
Xloc | location covariates: numeric vector of length \( p \)
window | maximum distance: non-negative real number
offset | numeric vector of length \( n \)
group | confounding variable: factor of length \( n \)
perm | number of iterations: positive integer
phi | dispersion parameters: vector of length \( q \)
kind | computation: number between 0 and 1

Value

The function returns a dataframe, with the p-value in the first column, and the test statistic in the second column.

References


See Also

This is an *internal* function. The user functions are *cursus*, *omnibus*, and *proprius*.

Examples

```r
# simulate high-dimensional data
n <- 30
q <- 10
p <- 100
set.seed(1)
Y <- matrix(rnbinom(q*n,mu=10,
                   size=1/0.25),nrow=q,ncol=n)
X <- matrix(rnorm(p*n),nrow=p,ncol=n)
Yloc <- seq(0,1,length.out=q)
Xloc <- seq(0,1,length.out=p)
window <- 1

# hypothesis testing
cursus(Y,Yloc,X,Xloc,window)
```
**Description**

This page lists and describes all internal functions of the R package `globalSeq`.

**Preparation**
- `intern.estim` estimates the parameters of the negative binomial distribution by maximum likelihood.
- `intern.permu` permutes values across samples, either across all samples or across samples within subgroups.
- `intern.score` computes the score test statistic.

**Testing**
- `intern.crude` calculates p-values by permutation.
- `intern.focus` calculates p-values by permutation, focusing on a region of interest.
- `intern.conva` calculates p-values by permutation, using the method of control variates.

**Decomposition**
- `intern.cov` decomposes the test statistic to show the influence of covariates.
- `intern.sam` decomposes the test statistic to show the influence of samples.
- `intern.plot` plots the contributions of covariates or samples.

**Communication**
- `intern.chromo` runs through all genes on a chromosome.
- `intern.select` identifies local covariates.
- `intern.matrix` transforms data to a numeric matrix.

**See Also**

The user functions of the R package `globalSeq` are `cursus`, `omnibus` and `proprius`.

---

**omnibus**

**Omnibus test**

**Description**

Test of association between a count response and one or more covariate sets. This test may be conceptualised as a test of overall significance in regression analysis, where the response variable is overdispersed, and where the number of explanatory variables (p) exceeds the sample size (n). The negative binomial distribution accounts for overdispersion and a random effect model accounts for high dimensionality (p>n).

**Usage**

```r
omnibus(y, X, offset = NULL, group = NULL,
       mu = NULL, phi = NULL,
       perm = 1000, kind = 1)
```
Arguments

- **response variable**: numeric vector of length $n$
- **one covariate set**: numeric matrix with $n$ rows (samples) and $p$ columns (covariates);
- **multiple covariate sets**: list of numeric matrices with $n$ rows (samples)
- **offset**: numeric vector of length $n$
- **group**: confounding variable: factor of length $n$
- **mu**: mean parameters: numeric vector of length 1 or $n$
- **phi**: dispersion parameter: non-negative real number
- **perm**: number of iterations: positive integer
- **kind**: computation: number between 0 and 1

Details

The user can provide a common $\mu$ for all samples or sample-specific $\mu$, and a common $\phi$. Setting $\phi$ equal to zero is equivalent to using the Poisson model. If $\mu$ is missing, then $\mu$ is estimated from $y$. If $\phi$ is missing, then $\mu$ and $\phi$ are estimated from $y$. The offset is only taken into account for estimating $\mu$ or $\phi$. By default the offset is `rep(1,n)`. The user can provide the **confounding** variable group. Note that each level of group must appear at least twice in order to allow stratified permutations.

Efficient alternatives to classical permutation ($\text{kind}=1$) are the method of control variates ($\text{kind}=0$) and permutation in chunks ($0 < \text{kind} < 1$) [details](#).

Value

The function returns a dataframe, with the p-value in the first column, and the test statistic in the second column.

References


See Also

The function `proprius` calculates the contributions of individual samples or covariates to the test statistic. The function `cursus` tests for association between RNA-Seq and local genetic or epigenetic alternations across the whole genome. All other functions of the R package `globalSeq` are internal.
Examples

```r
# simulate high-dimensional data
n <- 30; p <- 100
y <- rnbinom(n, mu=10, size=1/0.25)
X <- matrix(rnorm(n*p), nrow=n, ncol=p)

# hypothesis testing
omnibus(y, X)
```

<table>
<thead>
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<th>Decomposition</th>
</tr>
</thead>
</table>

Description

Even though the function `omnibus` tests a single hypothesis on a whole covariate set, this function allows to calculate the individual contributions of `n` samples or `p` covariates to the test statistic.

Usage

```r
proprius(y, X, type, offset = NULL, group = NULL,
         mu = NULL, phi = NULL,
         alpha = NULL, perm = 1000, plot = TRUE)
```

Arguments

- `y` **response variable**: numeric vector of length `n`
- `X` **covariate set**: numeric matrix with `n` rows (samples) and `p` columns (covariates)
- `type` character `'covariates'` or `'samples'`
- `offset` numeric vector of length `n`
- `group` confounding variable: factor of length `n`
- `mu` mean parameters: numeric vector of length 1 or `n`
- `phi` dispersion parameter: non-negative real number
- `alpha` significance level: real number between 0 and 1
- `perm` number of iterations: positive integer
- `plot` plot of results: logical

Details

The user can provide a common `mu` for all samples or sample-specific `mu`, and a common `phi`. Setting `phi` equal to zero is equivalent to using the Poisson model. If `mu` is missing, then `mu` is estimated from `y`. If `phi` is missing, then `mu` and `phi` are estimated from `y`. The `offset` is only taken into account for estimating `mu` or `phi`.

The user can provide the confounding variable `group`. Note that each level of `group` must appear at least twice in order to allow stratified permutations.
Value

If alpha=NULL, then the function returns a numeric vector, and else a list of numeric vectors.

References

A Rauschenberger, MA Jonker, MA van de Wiel, and RX Menezes (2016). "Testing for association between RNA-Seq and high-dimensional data", BMC Bioinformatics. 17:118. html pdf (open access)


See Also

The function omnibus tests for associations between an overdispersed response variable and a high-dimensional covariate set. The function cursus tests for association between RNA-Seq and local genetic or epigenetic alternations across the whole genome. All other functions of the R package globalSeq are internal.

Examples

```r
# simulate high-dimensional data
n <- 30; p <- 100
y <- rnbinom(n,mu=10,size=1/0.25)
X <- matrix(rnorm(n*p),nrow=n,ncol=p)

# decomposition
proprius(y,X,type="samples")
proprius(y,X,type="covariates")
```

Description

This dataset allows to reproduce the examples shown in the vignette.

Usage

data(toydata)

Format

A list of numeric vectors and numeric matrices.

Value

All entries are numeric.
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